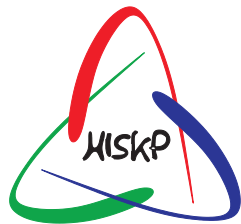


Status of the Bonn-Gatchina partial wave analysis

A. Anisovich

HISKP, Uni-Bonn (Bonn) and PNPI (Gatchina)



Topics

- **Data review**
- **Multipole decomposition of the single pion photoproduction amplitude**
- **$P_{11}(1/2^+)$ wave**
- **$P_{13}(3/2^+)$ wave**

Bonn-Gatchina PWA group

A. Anisovich, E. Klempt, V. Nikonov, A. Sarantsev and U. Thoma.

Aims of BnGa PWA

- **Aim: Determination of the full spectrum of baryon resonances and their decay modes**
- **Method: Simultaneous description of all relevant data for baryon spectroscopy**

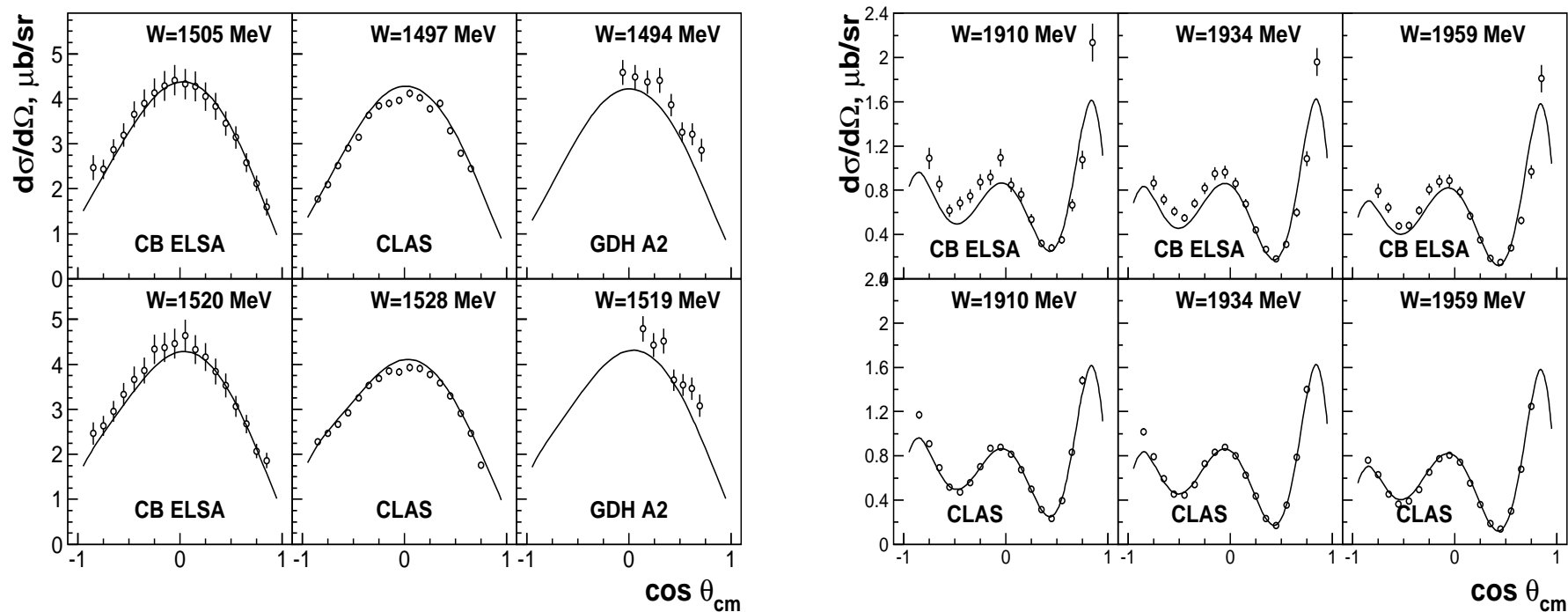
Pion induced reactions with recently included data sets.

Observable	N_{data}	$\frac{\chi^2}{N_{\text{data}}}$		Observable	N_{data}	$\frac{\chi^2}{N_{\text{data}}}$	
$N_{1/2-}^* S_{11}(\pi N \rightarrow \pi N)$	104	1.81	SAID	$\Delta_{1/2-} S_{31}(\pi N \rightarrow \pi N)$	112	2.27	SAID
$N_{1/2+}^* P_{11}(\pi N \rightarrow \pi N)$	112	2.49	SAID	$\Delta_{1/2+} P_{31}(\pi N \rightarrow \pi N)$	104	2.01	SAID
$N_{3/2+}^* P_{13}(\pi N \rightarrow \pi N)$	112	1.90	SAID	$\Delta_{3/2+}^* P_{33}(\pi N \rightarrow \pi N)$	120	2.53	SAID
$\Delta_{3/2-}^* D_{33}(\pi N \rightarrow \pi N)$	108	2.56	SAID	$N_{3/2-}^* D_{13}(\pi N \rightarrow \pi N)$	96	2.16	SAID
$N_{5/2-}^* D_{15}(\pi N \rightarrow \pi N)$	96	3.37	SAID	$\Delta_{5/2+} F_{35}(\pi N \rightarrow \pi N)$	62	1.32	SAID
$\Delta_{7/2+} F_{37}(\pi N \rightarrow \pi N)$	72	2.86	SAID				
$d\sigma/d\Omega(\pi^- p \rightarrow n\eta)$	70	1.96	Richards et al.	$d\sigma/d\Omega(\pi^- p \rightarrow n\eta)$	84	2.67	CBALL
$d\sigma/d\Omega(\pi^- p \rightarrow K\Lambda)$	479	1.55	RAL	$P(\pi^- p \rightarrow K\Lambda)$	261	1.76	RAL+ANL
$d\sigma/d\Omega(\pi^+ p \rightarrow K^+\Sigma)$	609	1.91	RAL	$P(\pi^+ p \rightarrow K^+\Sigma)$	420	2.74	RAL
$d\sigma/d\Omega(\pi^- p \rightarrow n\pi^0\pi^0)$			CBALL				

Single meson photoproduction reactions with recently included data sets.

Observable	N_{data}	$\frac{\chi^2}{N_{\text{data}}}$		Observable	N_{data}	$\frac{\chi^2}{N_{\text{data}}}$	
$d\sigma/d\Omega(\gamma p \rightarrow p\pi^0)$	1106	1.34	CB-ELSA	$d\sigma/d\Omega(\gamma p \rightarrow p\pi^0)$	861	1.46	GRAAL
$d\sigma/d\Omega(\gamma p \rightarrow p\pi^0)$	592	2.11	CLAS	$d\sigma/d\Omega(\gamma p \rightarrow p\pi^0)$	1692	1.25	TAPS@MAMI
$E(\gamma p \rightarrow p\pi^0)$	140	1.23	A2-GDH	$\Sigma(\gamma p \rightarrow p\pi^0)$	1492	3.26	SAID db
$P(\gamma p \rightarrow p\pi^0)$	607	3.23	SAID db	$\Gamma(\gamma p \rightarrow p\pi^0)$	389	3.71	SAID db
$H(\gamma p \rightarrow p\pi^0)$	71	1.26	SAID db	$G(\gamma p \rightarrow p\pi^0)$	75	1.50	SAID db
$O_x(\gamma p \rightarrow p\pi^0)$	7	1.77	SAID db	$O_z(\gamma p \rightarrow p\pi^0)$	7	0.46	SAID db
$d\sigma/d\Omega(\gamma p \rightarrow n\pi^+)$	1583	1.64	SAID db	$d\sigma/d\Omega(\gamma p \rightarrow n\pi^+)$	408	0.62	A2-GDH
$\Sigma(\gamma p \rightarrow n\pi^+)$	899	3.48	SAID db	$E(\gamma p \rightarrow n\pi^+)$	231	1.55	A2-GDH
$P(\gamma p \rightarrow n\pi^+)$	252	2.90	SAID db	$\Gamma(\gamma p \rightarrow n\pi^+)$	661	3.21	SAID db
$H(\gamma p \rightarrow p\pi^+)$	71	3.90	SAID db	$G(\gamma p \rightarrow p\pi^+)$	86	5.64	SAID db
$d\sigma/d\Omega(\gamma p \rightarrow p\eta)$	680	1.47	CB-ELSA	$d\sigma/d\Omega(\gamma p \rightarrow p\eta)$	100	2.16	TAPS
$\Sigma(\gamma p \rightarrow p\eta)$	51	2.26	GRAAL 98	$\Sigma(\gamma p \rightarrow p\eta)$	100	2.02	GRAAL 07
$T(\gamma p \rightarrow p\eta)$	50	1.48	Phoenix				

Comparison of different data sets on the $\gamma p \rightarrow \pi^0 p$ differential cross section, curve represents preliminary fit.



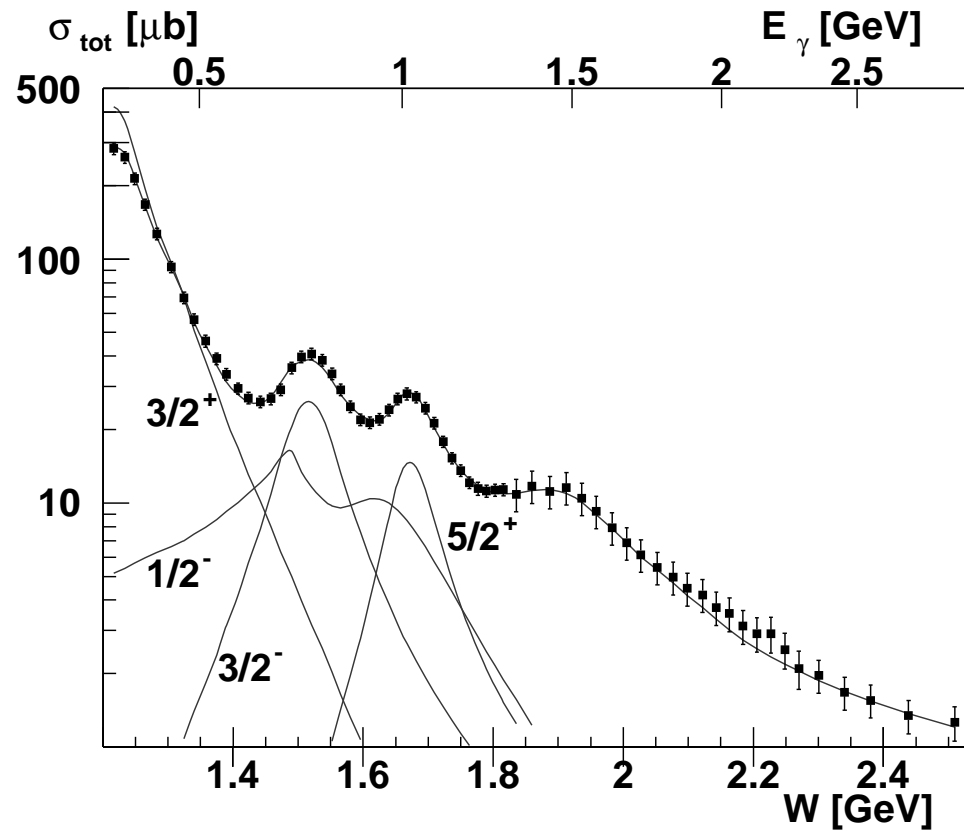
1. Free normalization factors (0.95-1.05) for each data sets are used;
2. Additional systematic errors are estimated and used in the fit

The fitted reactions. Recently included data sets.

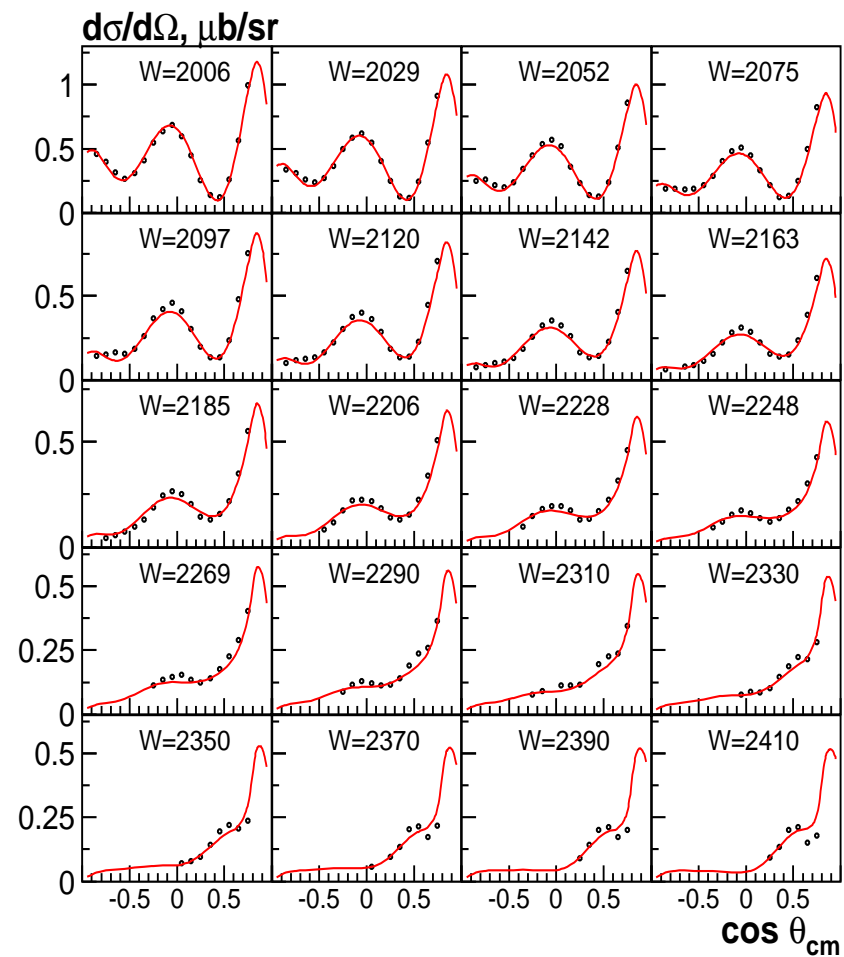
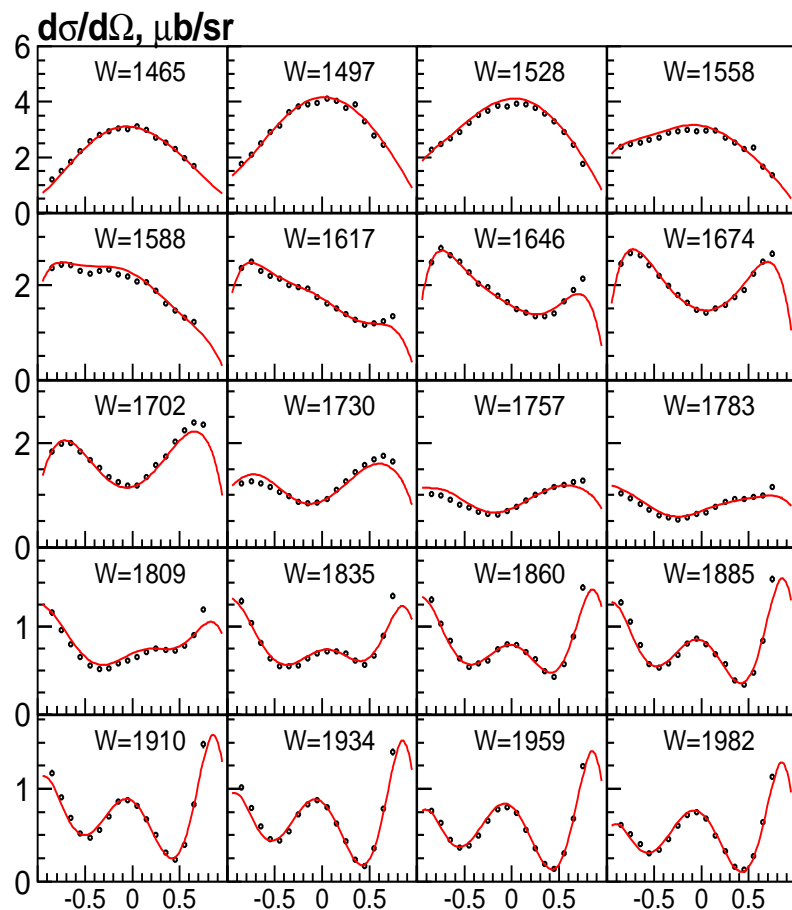
Observable	N_{data}	$\frac{\chi^2}{N_{\text{data}}}$		Observable	N_{data}	$\frac{\chi^2}{N_{\text{data}}}$	
$C_x(\gamma p \rightarrow \Lambda K^+)$	160	1.23	CLAS	$C_x(\gamma p \rightarrow \Sigma^0 K^+)$	94	2.20	CLAS
$C_z(\gamma p \rightarrow \Lambda K^+)$	160	1.41	CLAS	$C_z(\gamma p \rightarrow \Sigma^0 K^+)$	94	2.00	CLAS
$d\sigma/d\Omega(\gamma p \rightarrow \Lambda K^+)$	1377	1.81	CLAS	$d\sigma/d\Omega(\gamma p \rightarrow \Sigma^0 K^+)$	1280	2.06	CLAS
$P(\gamma p \rightarrow \Lambda K^+)$	202	2.03	CLAS	$P(\gamma p \rightarrow \Sigma^0 K^+)$	95	1.45	CLAS
$\Sigma(\gamma p \rightarrow \Lambda K^+)$	66	1.53	GRAAL	$\Sigma(\gamma p \rightarrow \Sigma^0 K^+)$	42	0.90	GRAAL
$\Sigma(\gamma p \rightarrow \Lambda K^+)$	45	1.65	LEP	$\Sigma(\gamma p \rightarrow \Sigma^0 K^+)$	45	1.11	LEP
$T(\gamma p \rightarrow \Lambda K^+)$	66	1.26	GRAAL 09	$d\sigma/d\Omega(\gamma p \rightarrow \Sigma^+ K^0)$	48	3.76	CLAS
$O_x(\gamma p \rightarrow \Lambda K^+)$	66	1.30	GRAAL 09	$d\sigma/d\Omega(\gamma p \rightarrow \Sigma^+ K^0)$	160	0.98	CB-ELSA
$O_z(\gamma p \rightarrow \Lambda K^+)$	66	1.54	GRAAL 09	$P(\gamma p \rightarrow \Sigma^+ K^0)$	72	0.61	CB-ELSA
$d\sigma/d\Omega(\gamma p \rightarrow p\pi^0\pi^0)$	CB-ELSA (1.4 GeV)			$E(\gamma p \rightarrow p\pi^0\pi^0)$	16	1.91	MAMI
$d\sigma/d\Omega(\gamma p \rightarrow p\pi^0\eta)$	CB-ELSA (3.2 GeV)			$\Sigma(\gamma p \rightarrow p\pi^0\eta)$	180	2.37	GRAAL
$d\sigma/d\Omega(\gamma p \rightarrow p\pi^0\pi^0)$	CB-ELSA (3.2 GeV)			$\Sigma(\gamma p \rightarrow p\pi^0\pi^0)$	128	0.96	GRAAL

$\gamma p \rightarrow \pi^0 p$ from Crystal Barrel at ELSA ($E_\gamma \leq 3.2$ GeV)

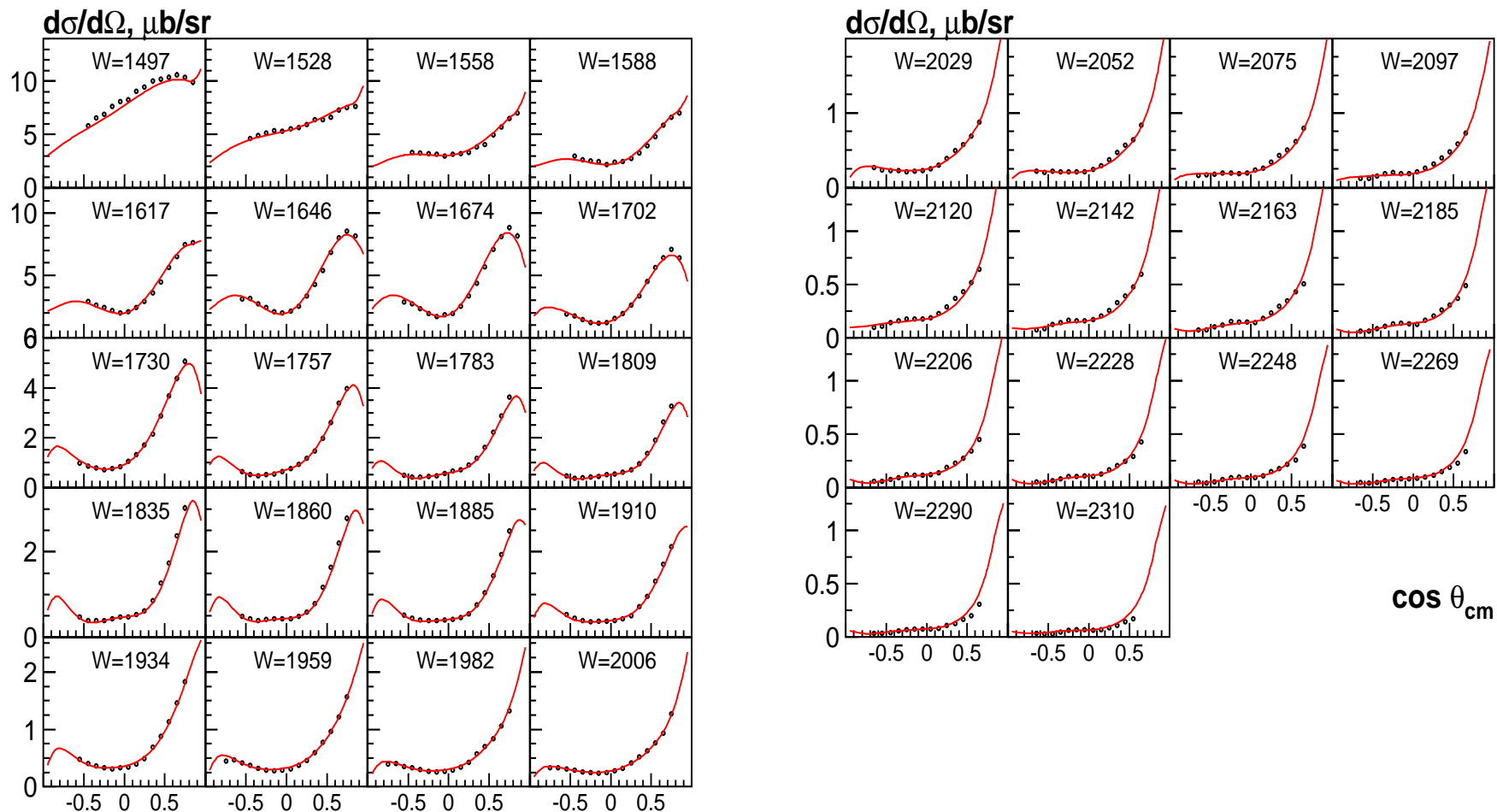
- $\Delta(1232)P_{33}$
- $N(1520)D_{13}$
- $N(1535)S_{11}$
- $N(1650)S_{11}$
- $N(1680)F_{15}$
- $\Delta(1700)D_{33}$
- $\Delta(1920)P_{33}$



CLAS 07 data on the differential cross section for $\gamma p \rightarrow \pi^0 p$ with current solution. Only statistical errors for the CLAS data are shown.



CLAS 09 data on the differential cross section for $\gamma p \rightarrow \pi^+ n$ with current solution.
Only statistical errors for the CLAS data are shown.

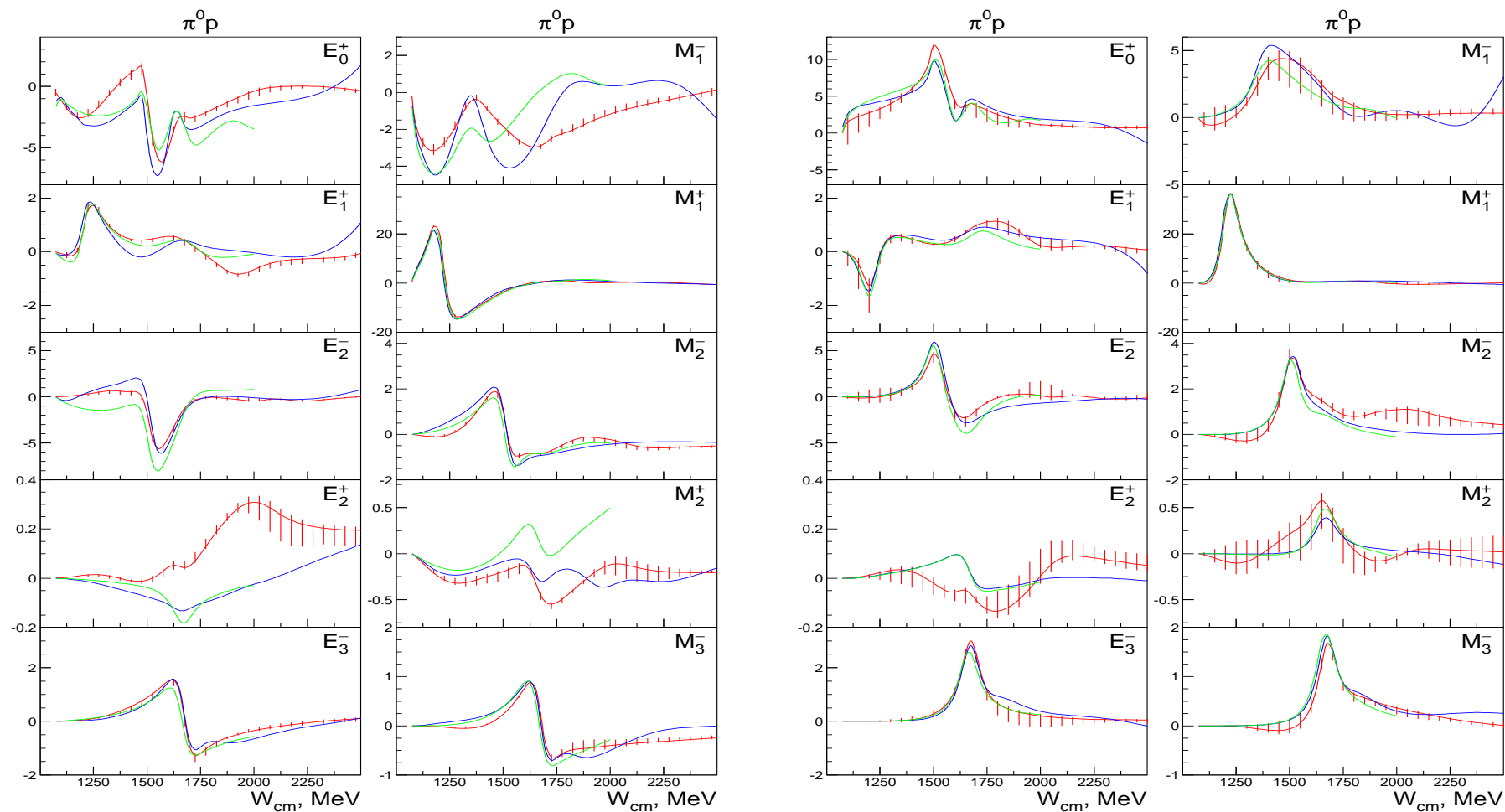


Photoproduction multipoles and partial waves. In general, two multipoles lead to one spin-parity wave.

Multipoles		Partial waves		J^P
E_0^+	-	S_{11}	S_{31}	$1/2^-$
-	M_1^-	P_{11}	P_{31}	$1/2^+$
E_1^+	M_1^+	P_{13}	P_{33}	$3/2^+$
E_2^-	M_2^-	D_{13}	D_{33}	$3/2^-$
E_2^+	M_2^+	D_{15}	D_{35}	$5/2^-$
E_3^-	M_3^-	F_{15}	F_{35}	$5/2^+$

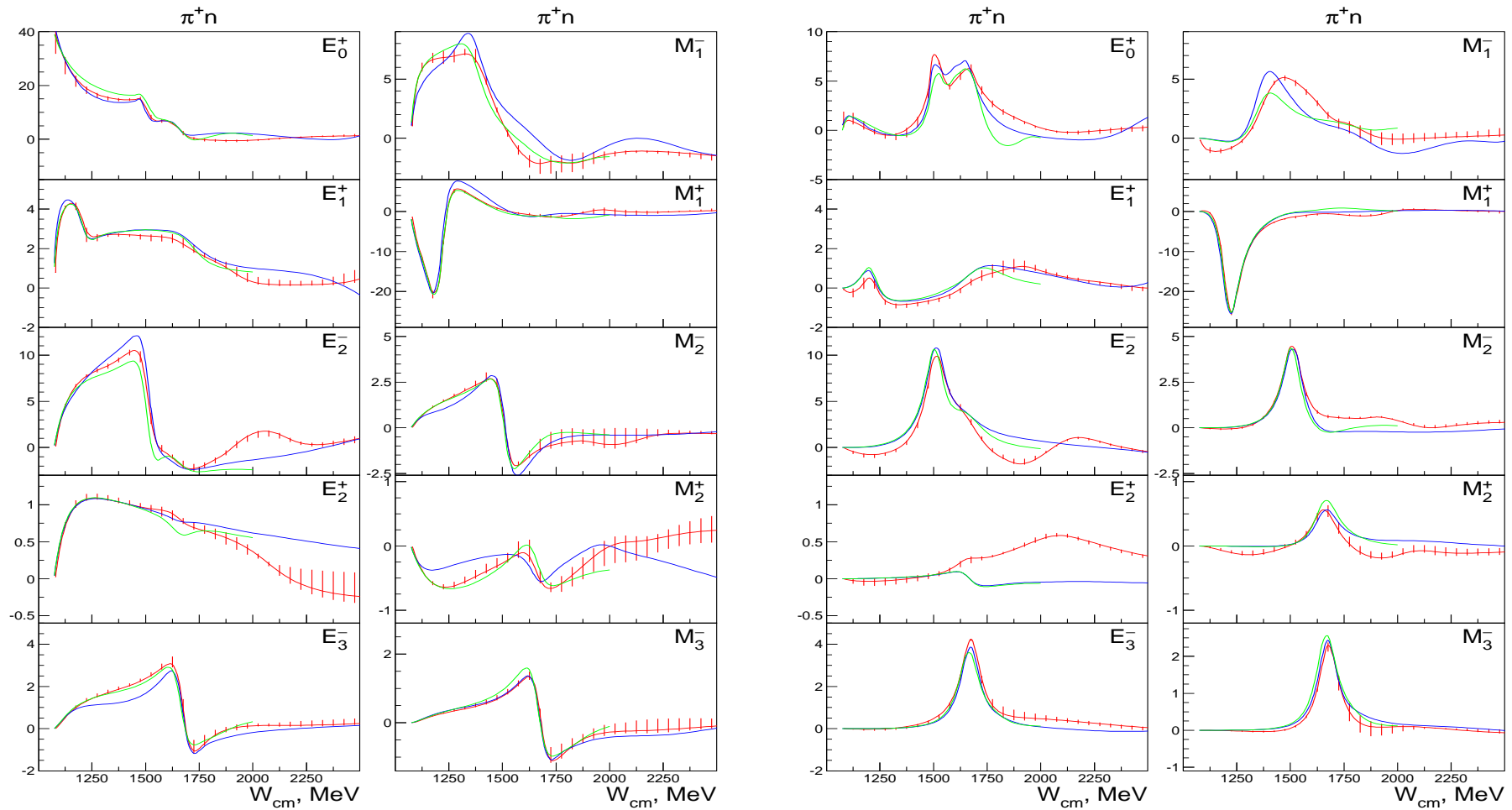
Real (left) and imaginary (right) parts of multipoles for the π^0 photoproduction.

Red - BoGa solution, blue - SAID, MAID 2009.



Real (left) and imaginary (right) parts of multipoles for the π^+ photoproduction.

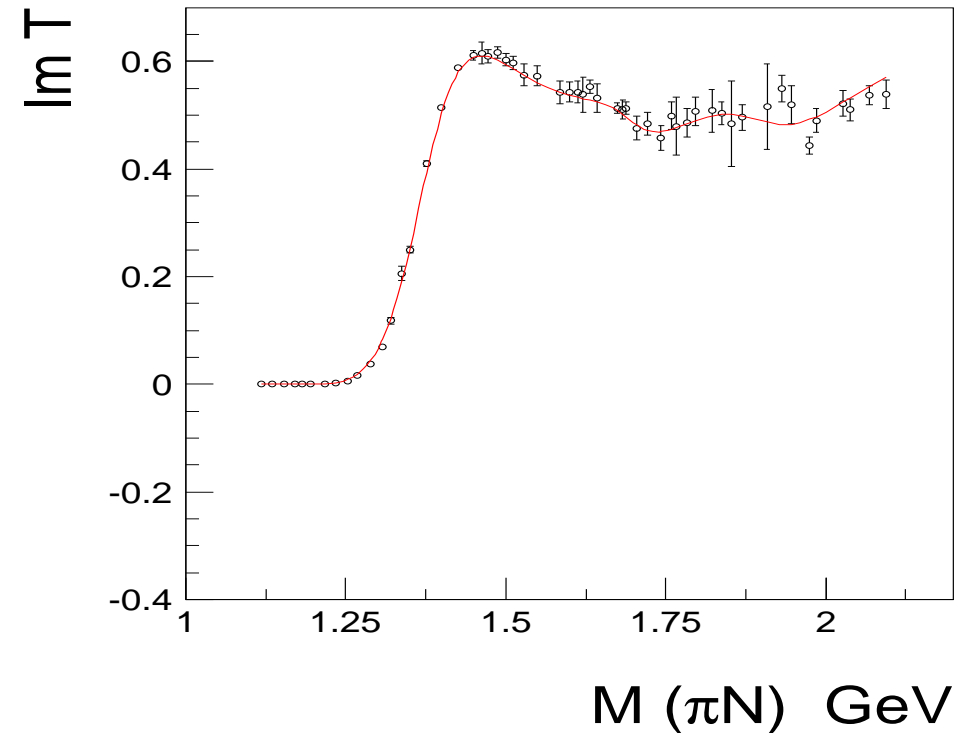
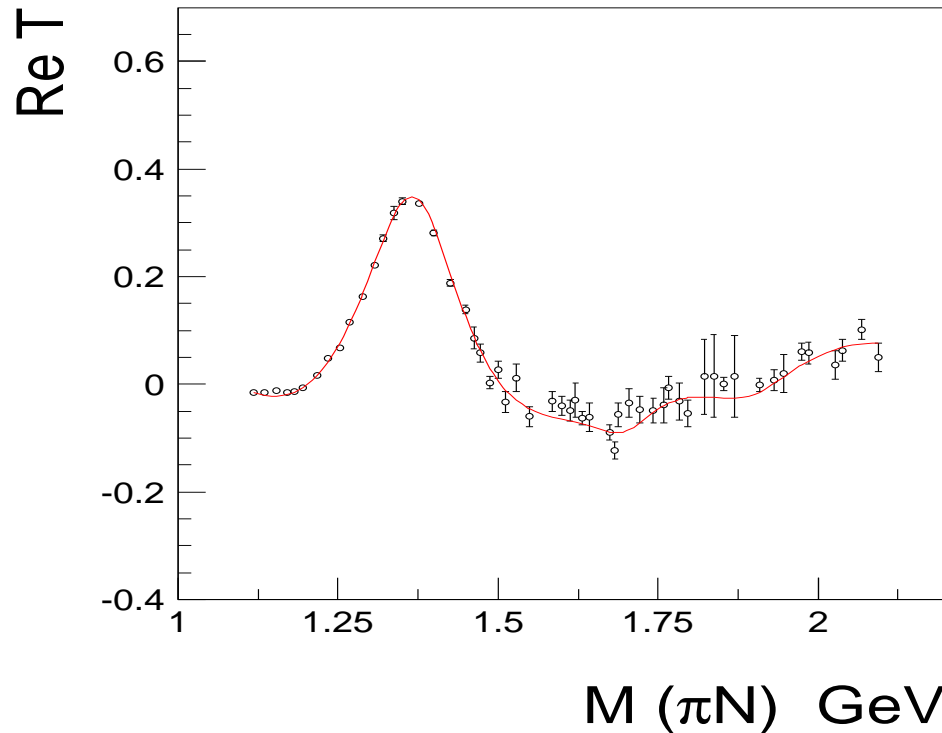
Red - BoGa solution, blue - SAID, MAID 2009.



$N\pi \rightarrow N\pi P_{11}$ wave (3 pole 4 channel K-matrix)

P_{11}

P_{11}

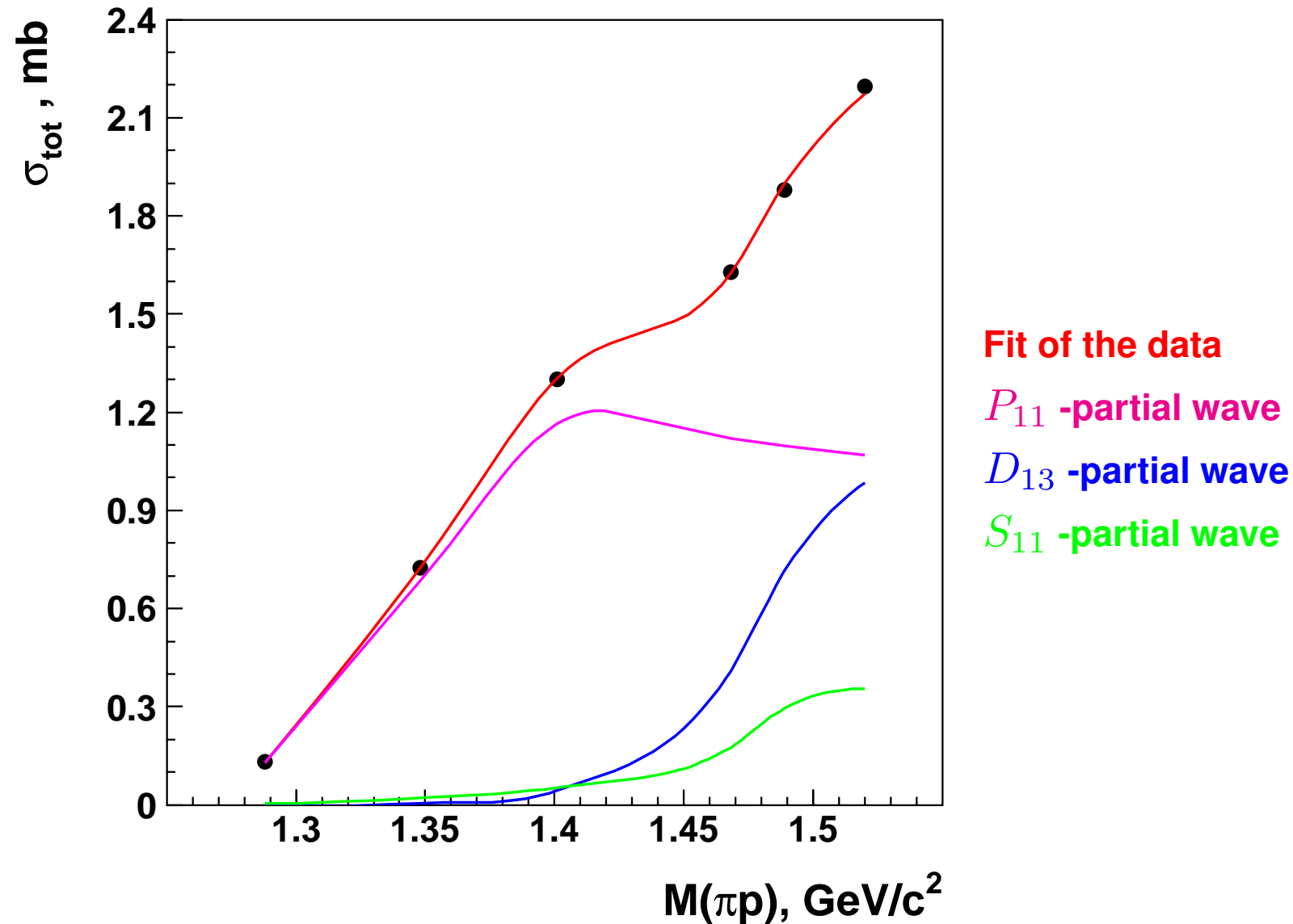


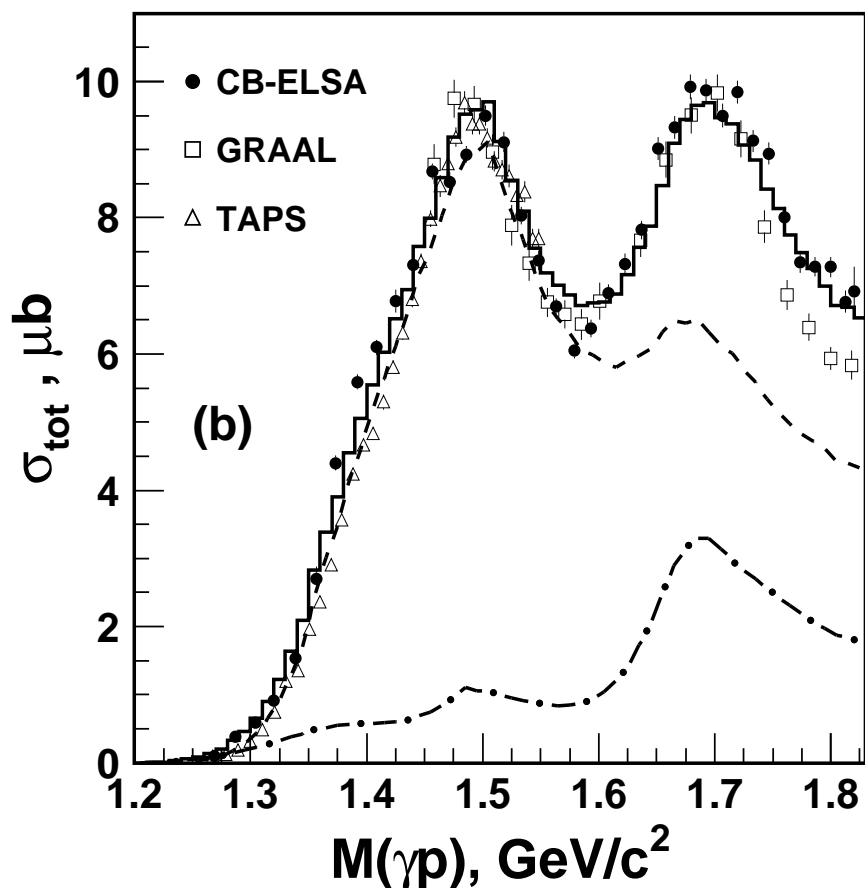
T-matrix poles (our fit and PDG value):

$M = 1370 \pm 4$ (1365 \pm 15) MeV, $-2 Im = 193 \pm 7$ (190 \pm 30) MeV;

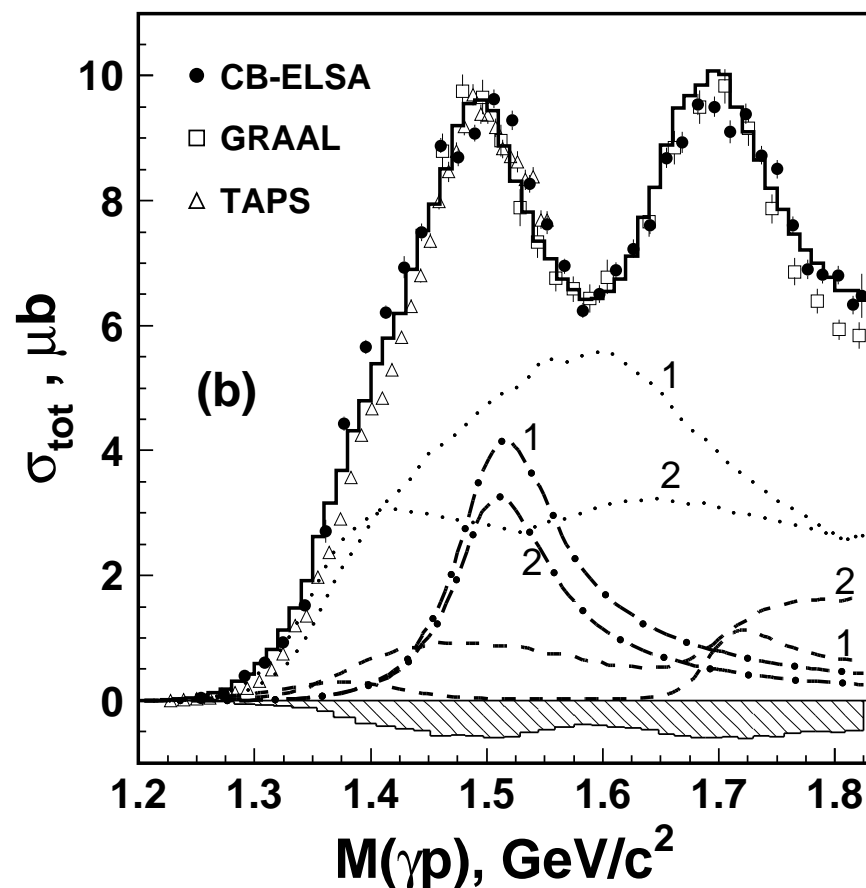
$M = 1708 \pm 18$ (1720 \pm 50) MeV, $-2 Im = 200 \pm 20$ (230 \pm 150) MeV;

$M = 1870 \pm 30$ MeV, $-2 Im = 280 \pm 80$ MeV

$\pi^- p \rightarrow n\pi^0\pi^0$ (Crystal Ball) total cross section

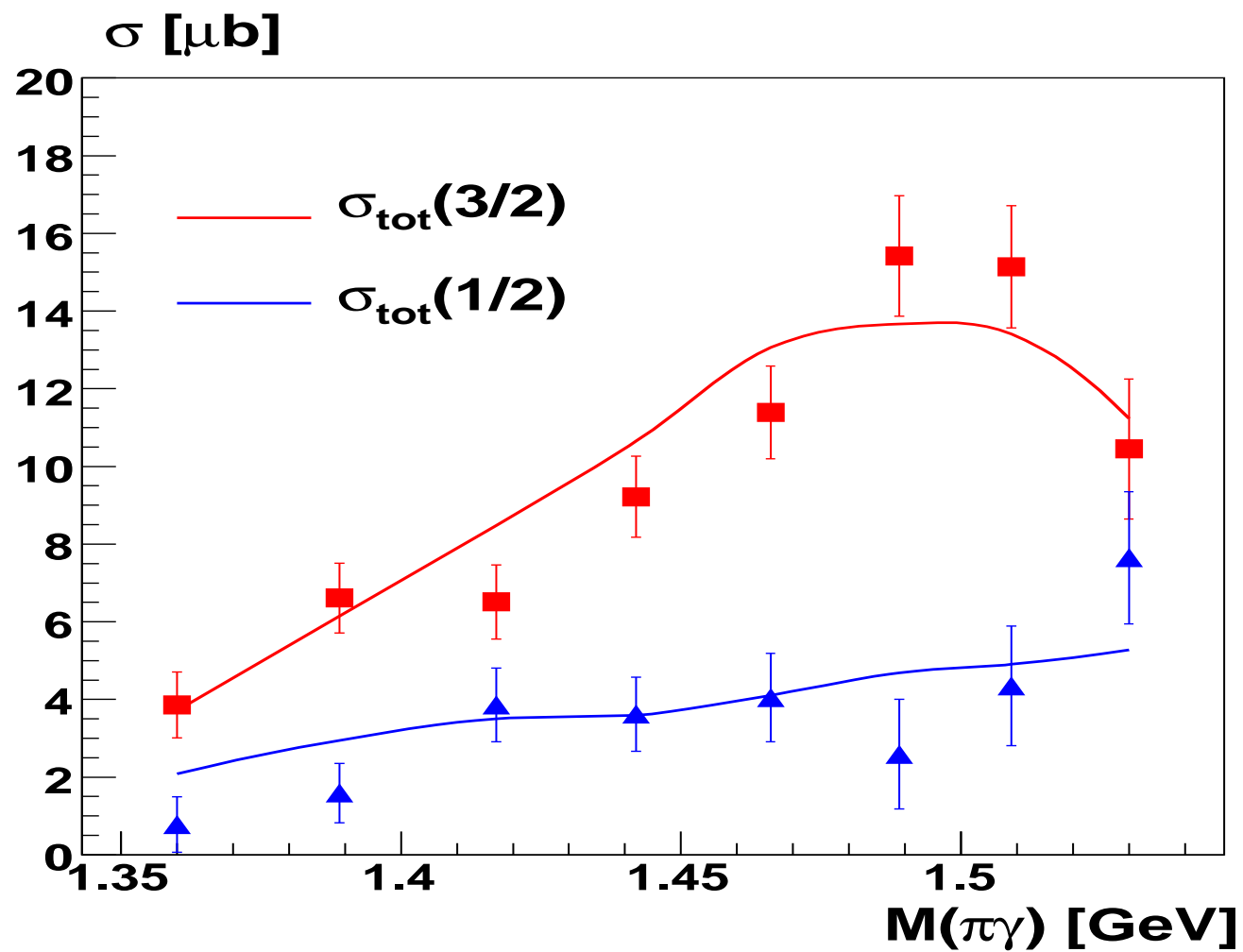
$$\gamma p \rightarrow p\pi^0\pi^0 \text{ (CB-ELSA) M.Fuchs et al.}$$


PWA corrected cross section and contributions from $\Delta(1232)\pi$ (dashed) and $N\sigma$ (dashed-dotted) final states.



Contributions from D_{33} (dotted), P_{11} (dashed) and D_{13} (dashed-dotted) partial waves.

The $\gamma p \rightarrow \pi^0 \pi^0 p$ helicity 3/2 and 1/2 differential cross sections

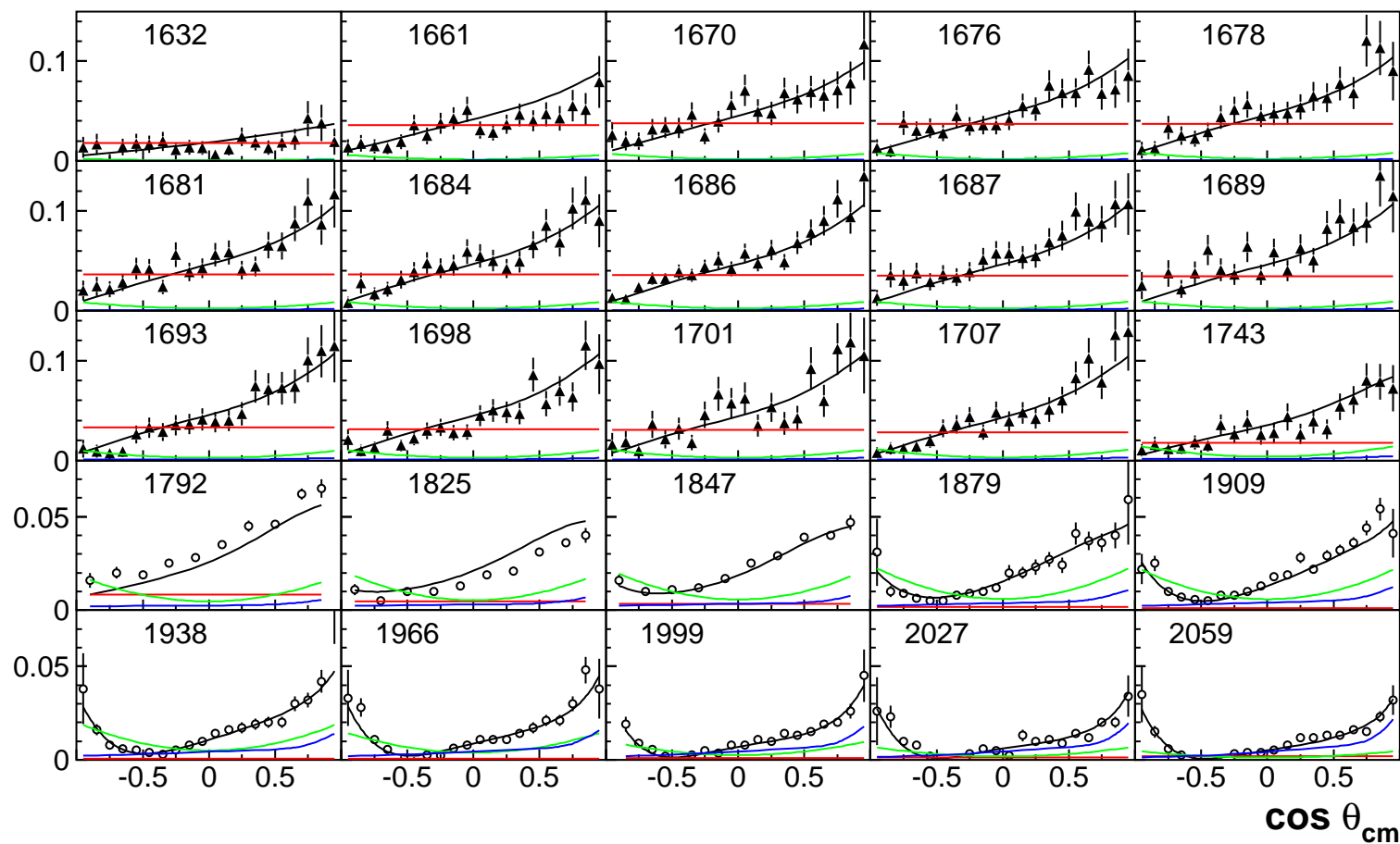


Properties of $N(1440)P_{11}$. The left column lists mass, width, partial widths of the Breit-Wigner resonance; the right column stands for pole position and squared couplings to the final state at the pole position.

M	=	$1436 \pm 15 \text{ MeV}$	M_{pole}	=	$1371 \pm 7 \text{ MeV}$
Γ	=	$335 \pm 40 \text{ MeV}$	Γ_{pole}	=	$192 \pm 20 \text{ MeV}$
$\Gamma_{\pi N}$	=	$205 \pm 25 \text{ MeV}$	$g_{\pi N}$	=	$(0.51 \pm 0.05) \cdot e^{-i\pi \frac{(35 \pm 5)}{180}}$
$\Gamma_{\sigma N}$	=	$71 \pm 17 \text{ MeV}$	$g_{\sigma N}$	=	$(0.82 \pm 0.16) \cdot e^{-i\pi \frac{(20 \pm 13)}{180}}$
$\Gamma_{\pi \Delta}$	=	$59 \pm 15 \text{ MeV}$	$g_{\pi \Delta}$	=	$(-0.57 \pm 0.08) \cdot e^{i\pi \frac{(25 \pm 20)}{180}}$
T-matrix:		$A_{1/2} = 0.055 \pm 0.020 \text{ GeV}$	$\phi = (70 \pm 30)^\circ$		

$P_{11}(1710)$ resonance

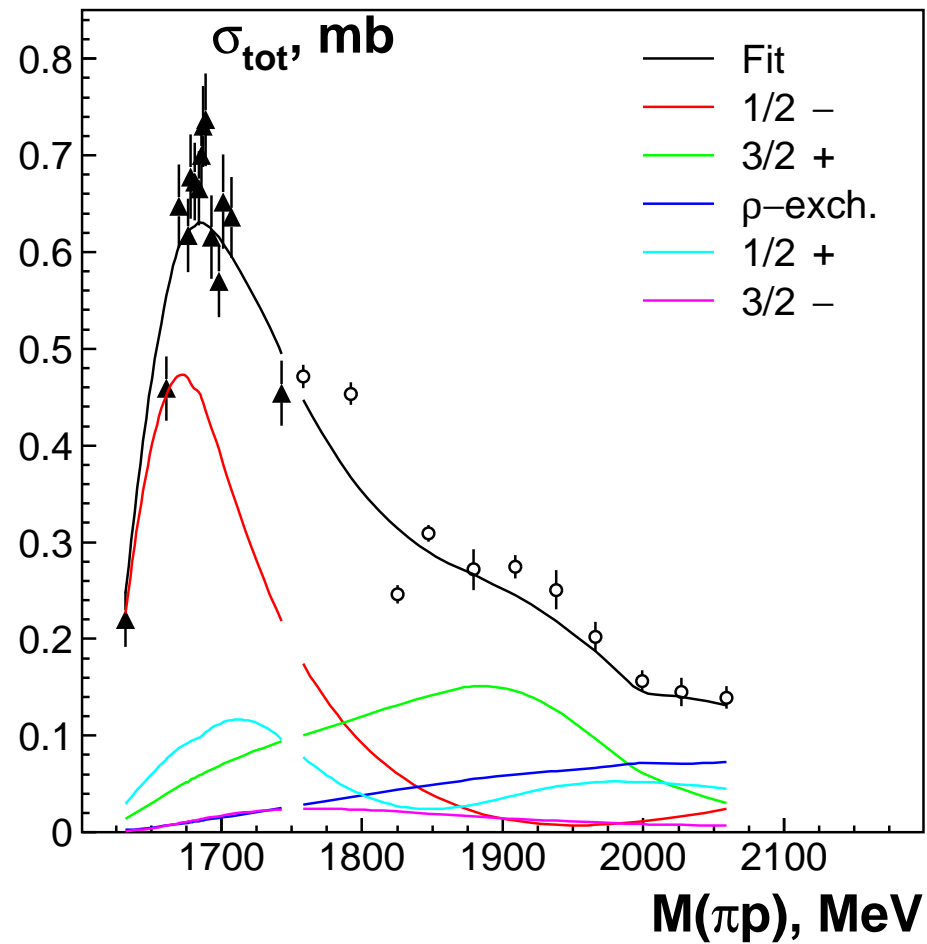
The differential cross section for the $\pi^- p \rightarrow K \Lambda$ reaction shows a clear contribution from this state ($S_{11} - P_{11}$ interference):



Preliminary fit

$P_{11}(1710)$ resonance

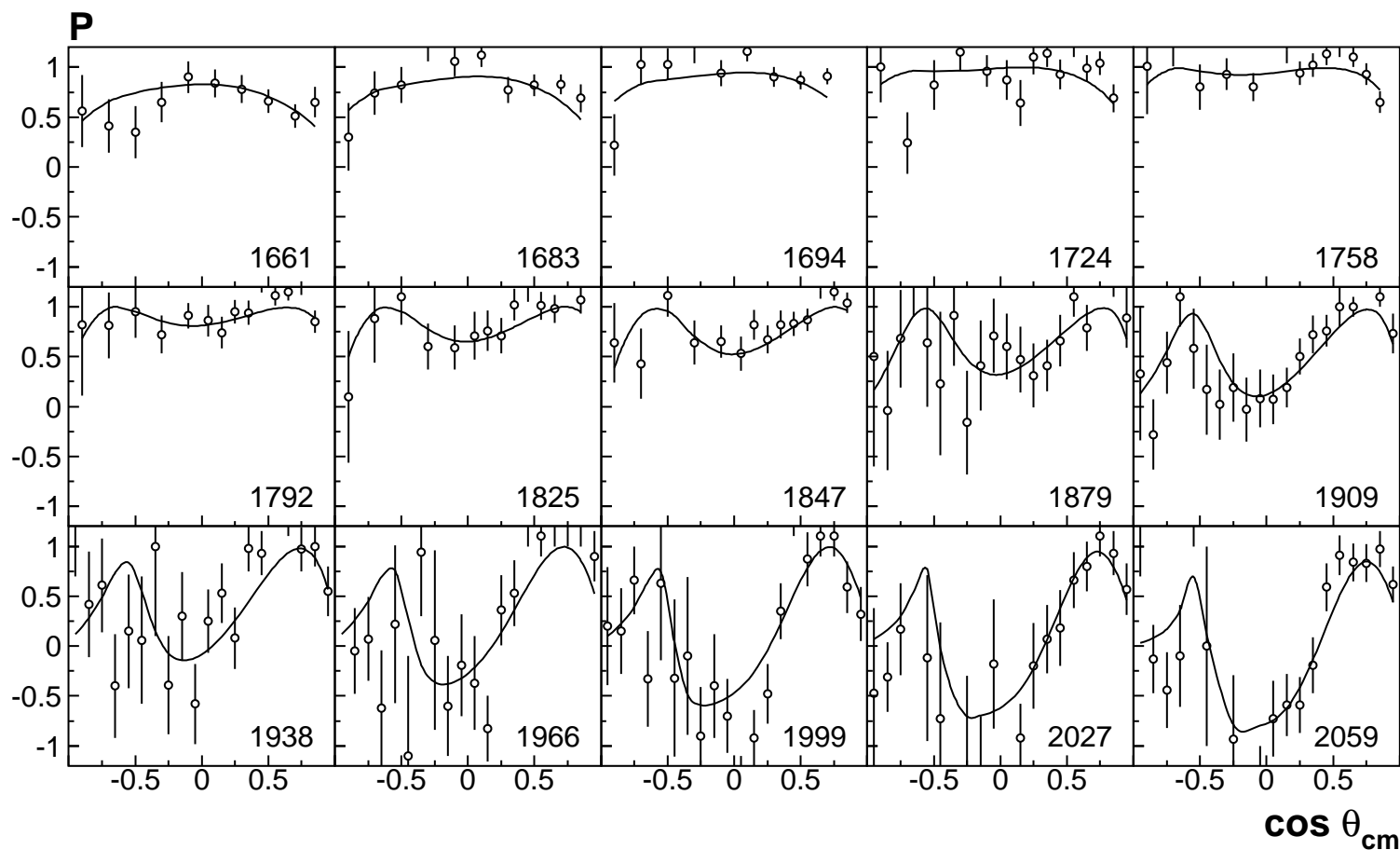
The total cross section for the $\pi^- p \rightarrow K \Lambda$ reaction:



Preliminary result

$P_{11}(1710)$ resonance

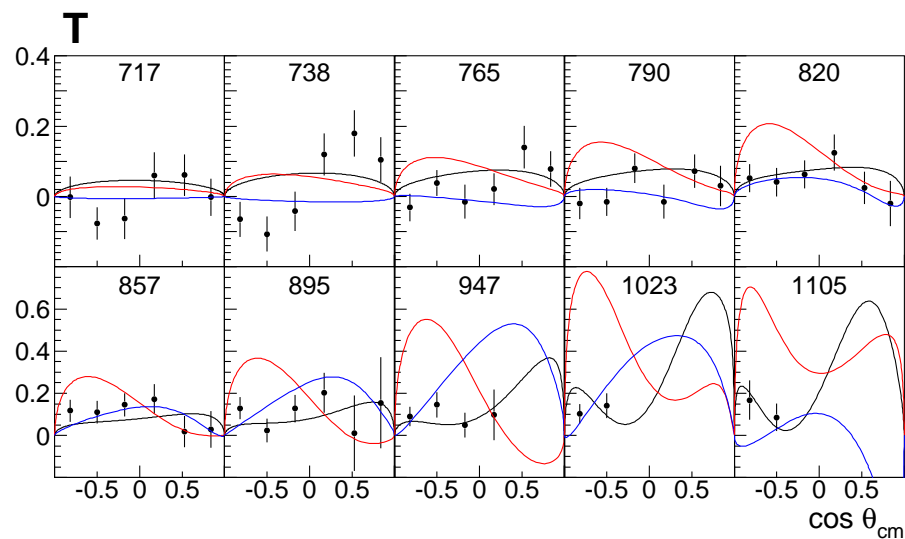
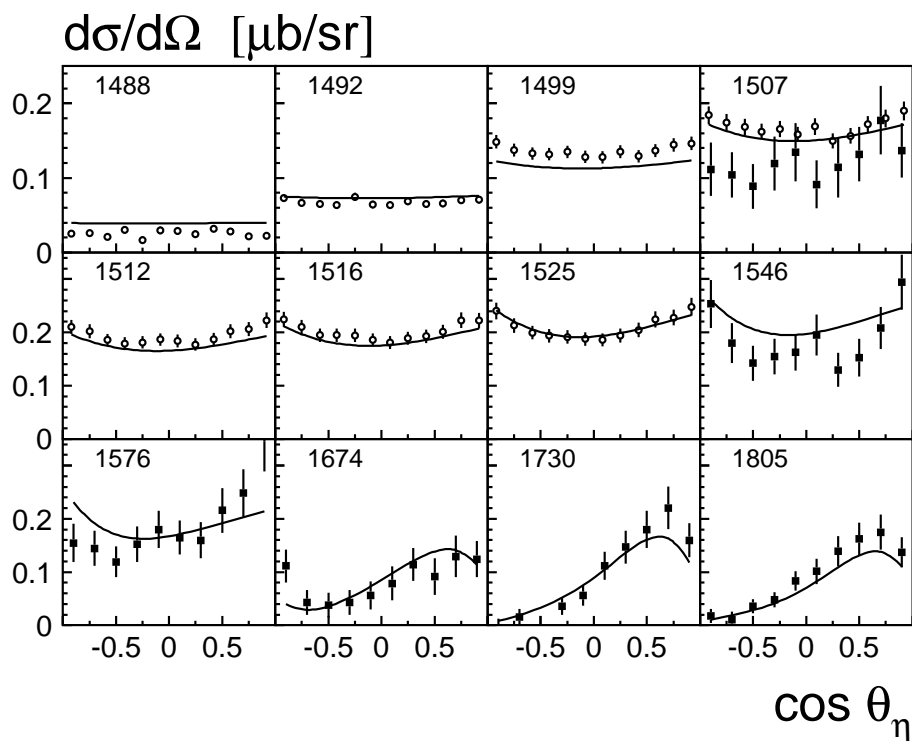
The recoil asymmetry for the $\pi^- p \rightarrow K \Lambda$ reaction. also shows a clear contribution from this state:

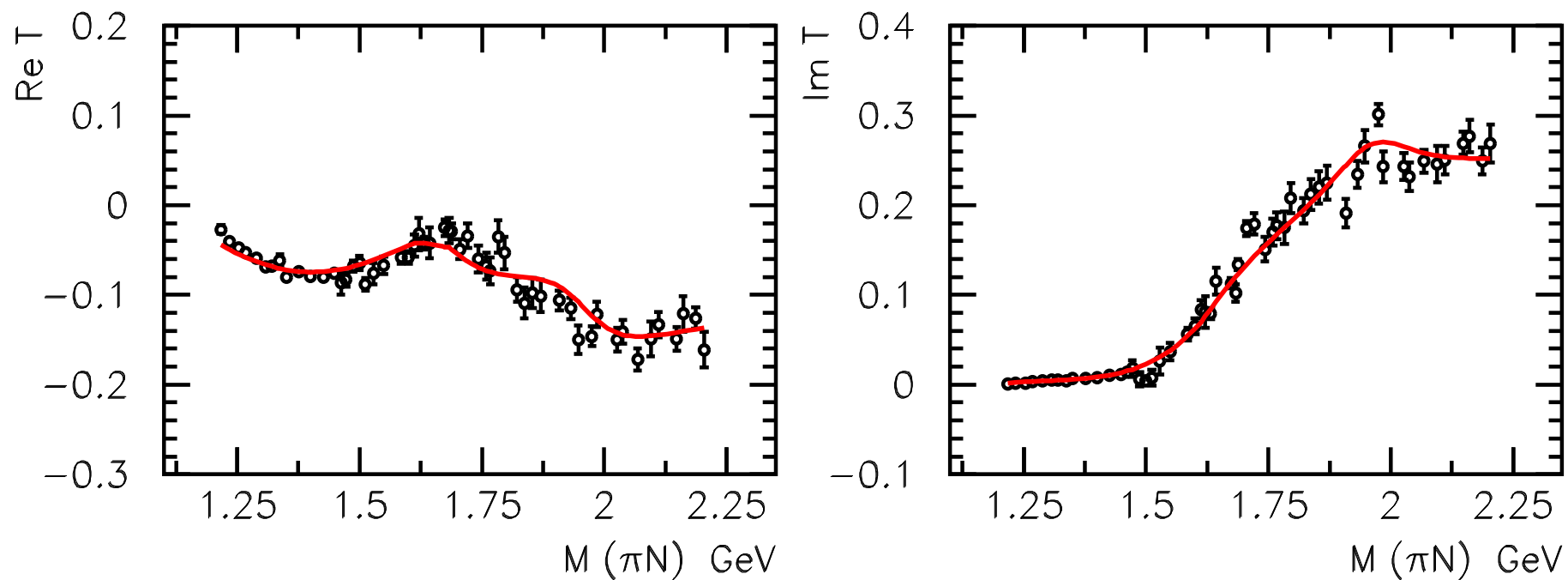


Preliminary fit

$P_{11}(1710)$ resonance

The data on $\pi^- p \rightarrow \eta n$ and the target asymmetry $\gamma p \rightarrow \eta p$ fix the position and couplings of $P_{11}(1710)$ state and reduce ηN coupling of the $P_{13}(1720)$ state.



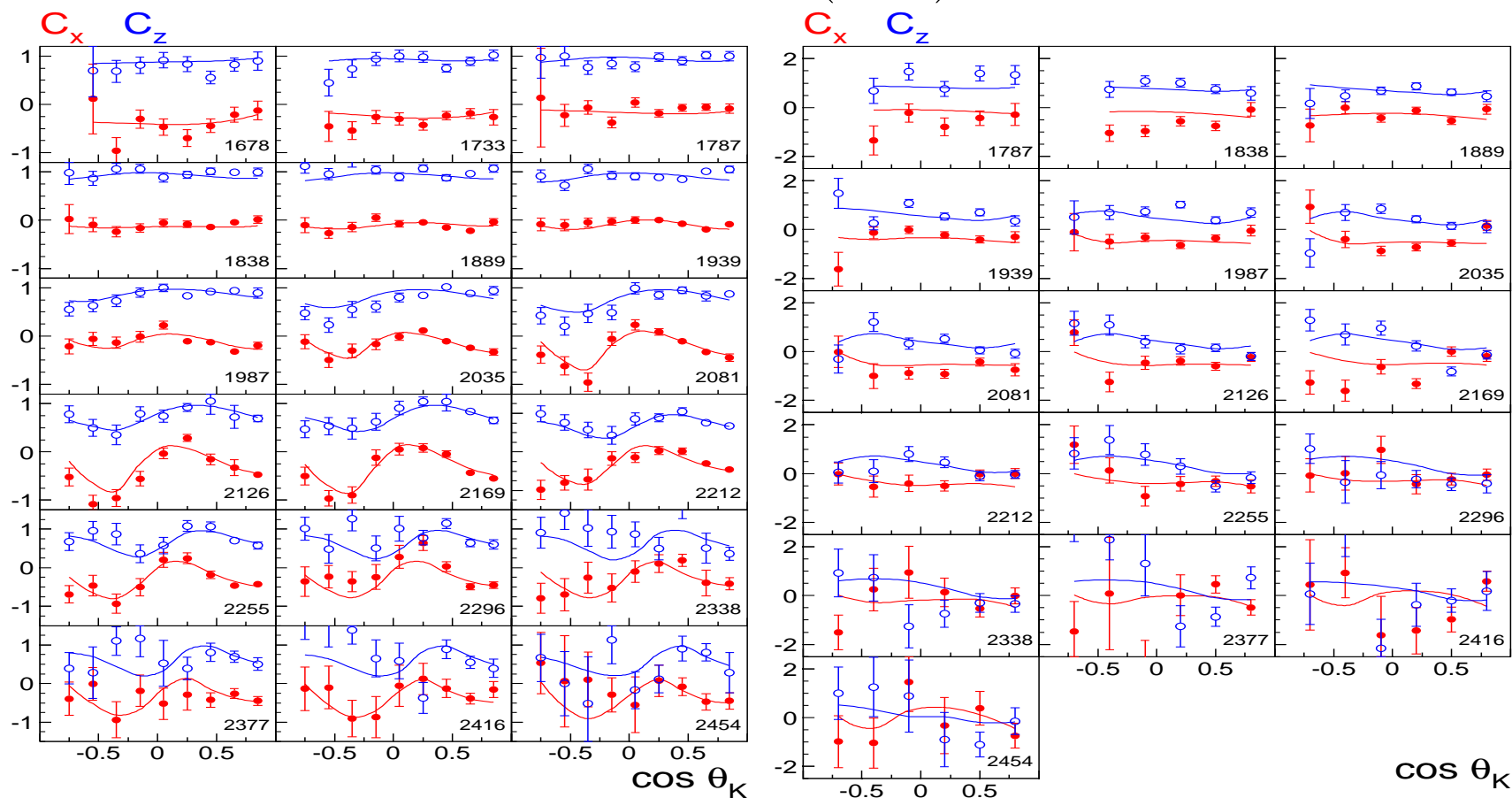
$N\pi \rightarrow N\pi$, P_{13} wave (3 pole 8 channel K-matrix)

2nd T-matrix poles: $M = 1960 \pm 20$ MeV, $2 \text{ Im} = 195 \pm 45$ MeV;

$P_{13}(1900)$ resonance

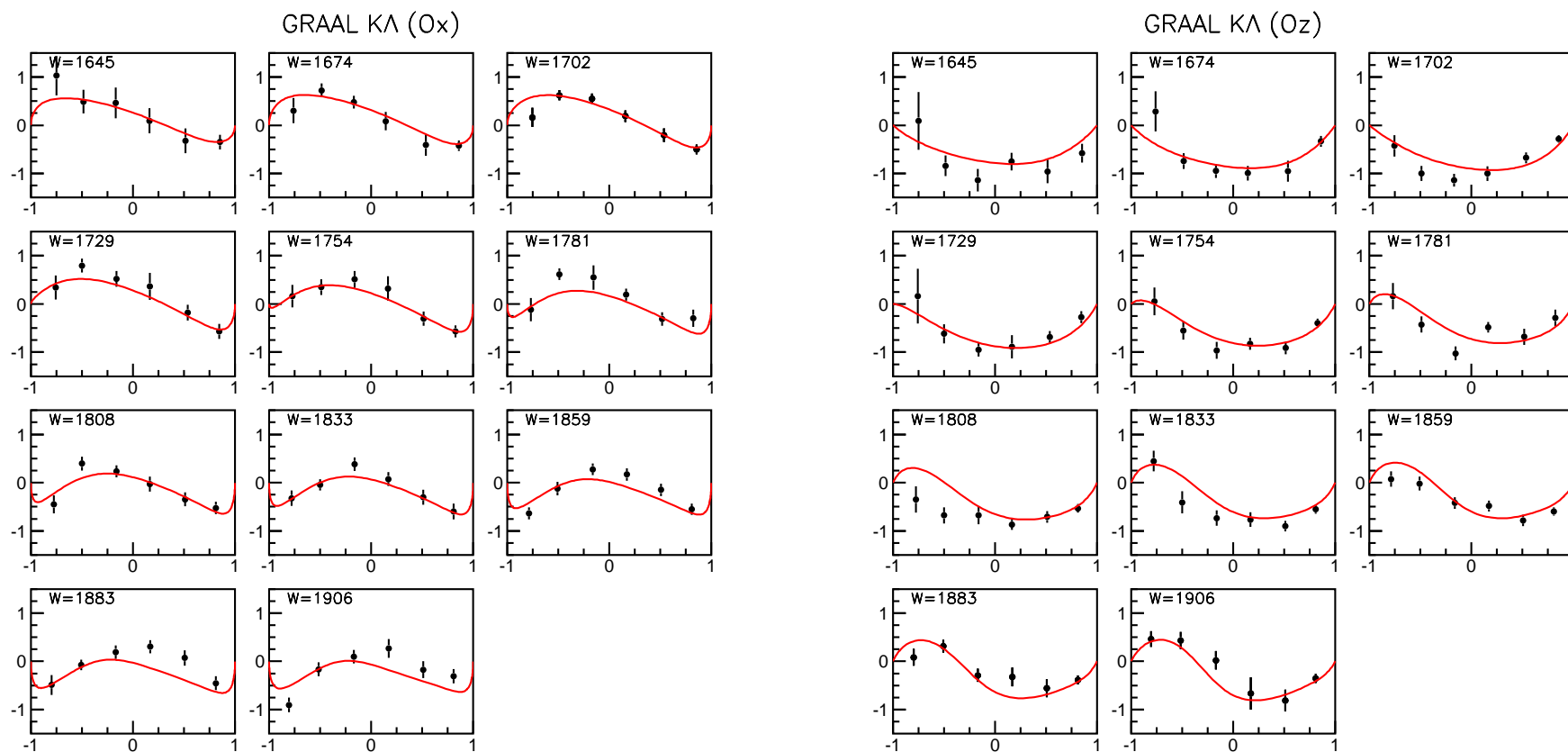
For $\gamma p \rightarrow K \Lambda$ (left) and $\gamma p \rightarrow K \Sigma$ (right) we have almost complete photoproduction experiment: σ (CLAS, SAPHIR), Σ (GRAAL, LEP), P (CLAS), C_x, C_z (CLAS), T, O_x, O_z (GRAAL).

The C_x and C_z data can be explained with $P_{13}(1900)$.



$P_{13}(1900)$ resonance

The solution is supported by the new GRALL data on O_x , O_z and T -observables: an important step to a complete experiment.



Summary

1. An approach for the combined analysis of the pion and photo induced reaction with two and multiparticle final states is developed.
2. The combined analysis of more than 75 different reactions helped us to identify the properties of known baryons.
3. The new data support the two new baryon states observed in hyperon photoproduction of $P_{11}(1880)$ and $P_{13}(1900)$.
4. The η -photoproduction data reveal the baryon resonance $D_{15}(2070)$.
5. The $D_{33}(1940)$ state is needed for the description of the $\gamma p \rightarrow \pi^0 \eta p$ data.
6. The data on $\pi^- p \rightarrow \eta n$ and $\pi^- p \rightarrow K^0 \Sigma$ support an existence of $P_{11}(1710)$.
7. The spectrum of observed states is in direct contradiction with a classical quark model. The best explanations are chiral symmetry reconstruction or AdS/QCD soft-wall model (see talk of E.Klempt).